# Natural Language Processing
# CSCI 4152/6509 — Lecture 17
# Deep Learning Architectures for NLP

Instructors: Vlado Keselj
Time and date: 14:35 – 15:55, 27-Nov-2025
Location: Studley LSC-Psychology P5260

# Previous Lecture

**Neural Network Models**

- Neural networks and deep learning
- Overview of Large Language Models
- Foundations of Deep Learning
  - From Naïve Bayes to Perceptron
- Perceptron as an Artificial Neuron and Computation
- Feedforward Neural Network and Matrix Computation

# P0 Topics Discussion (4)

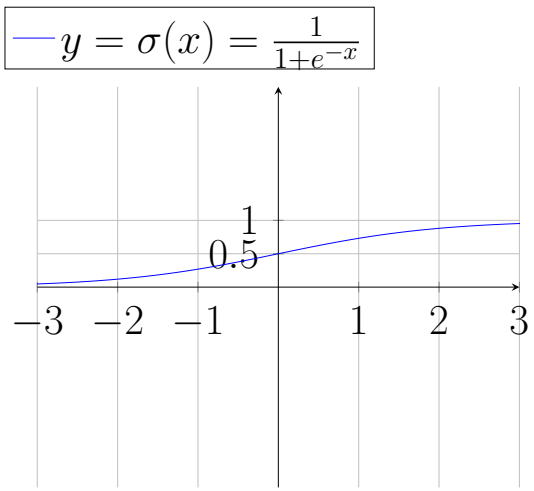
- Additional discussion of individual projects as proposed in P0 submissions (part 4)
- Projects discussed: P-18

# Activation Function

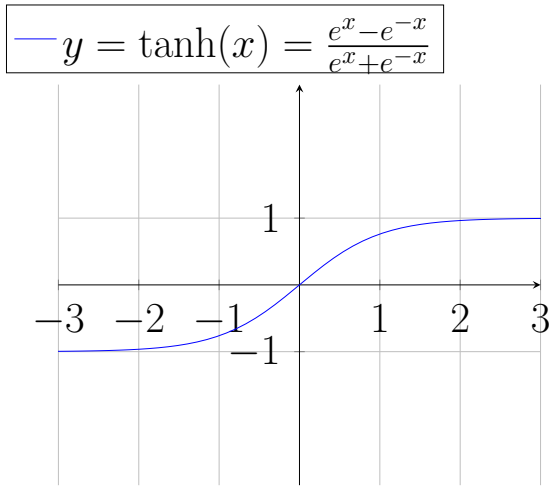
- must be non-linear
  - otherwise, the whole neural network would collapse into one neuron
- should be monotonically non-decreasing
- useful to be differentiable and relatively simple for speed of training
- Best known activation functions: sigmoid, tanh, ReLU (Rectified Linear Unit)

# Common Activation Functions

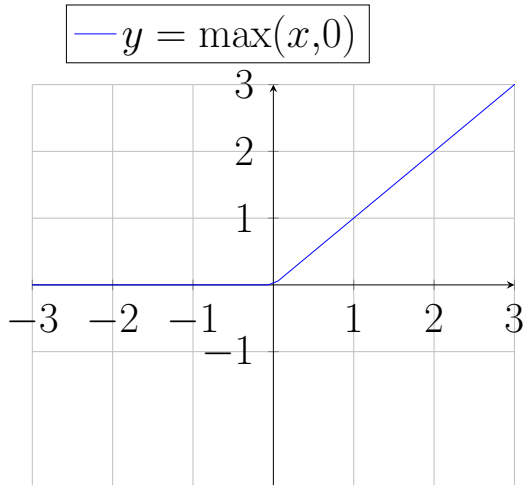
## Sigmoid




## tanh

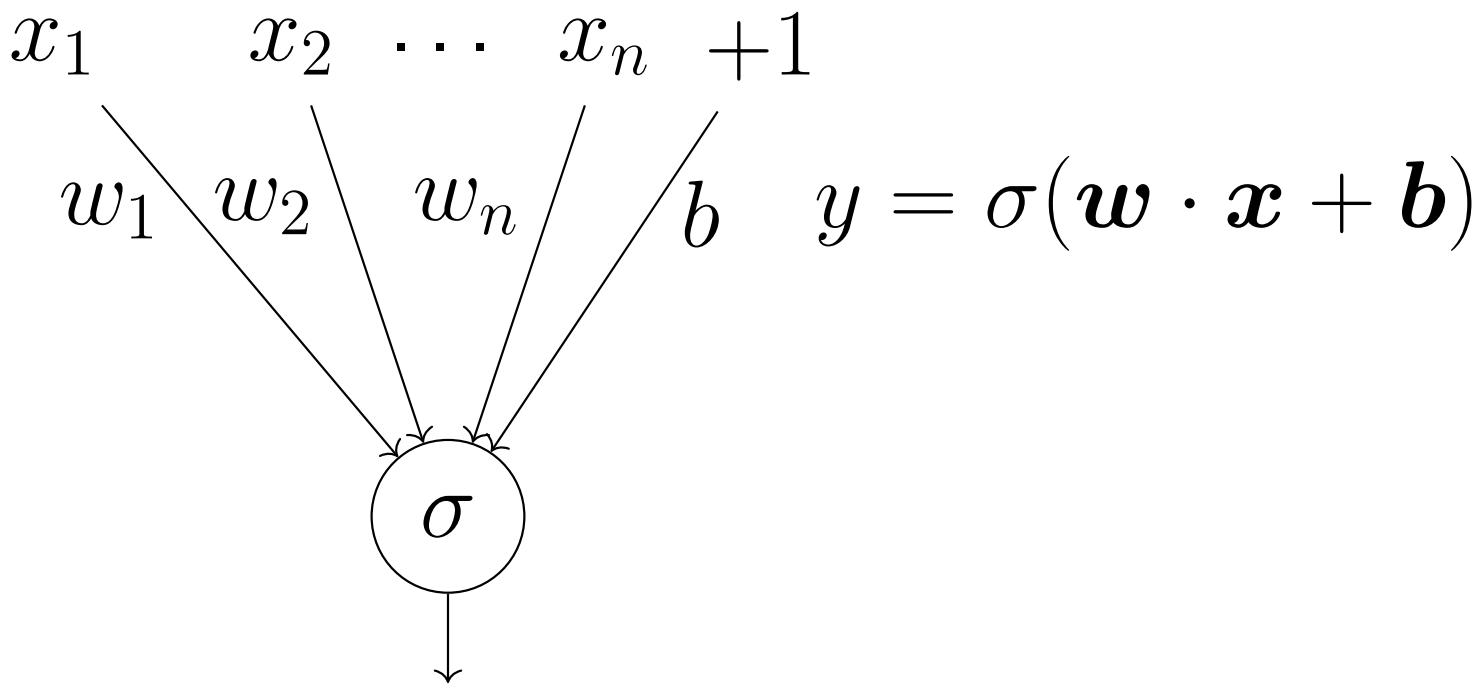



## ReLU



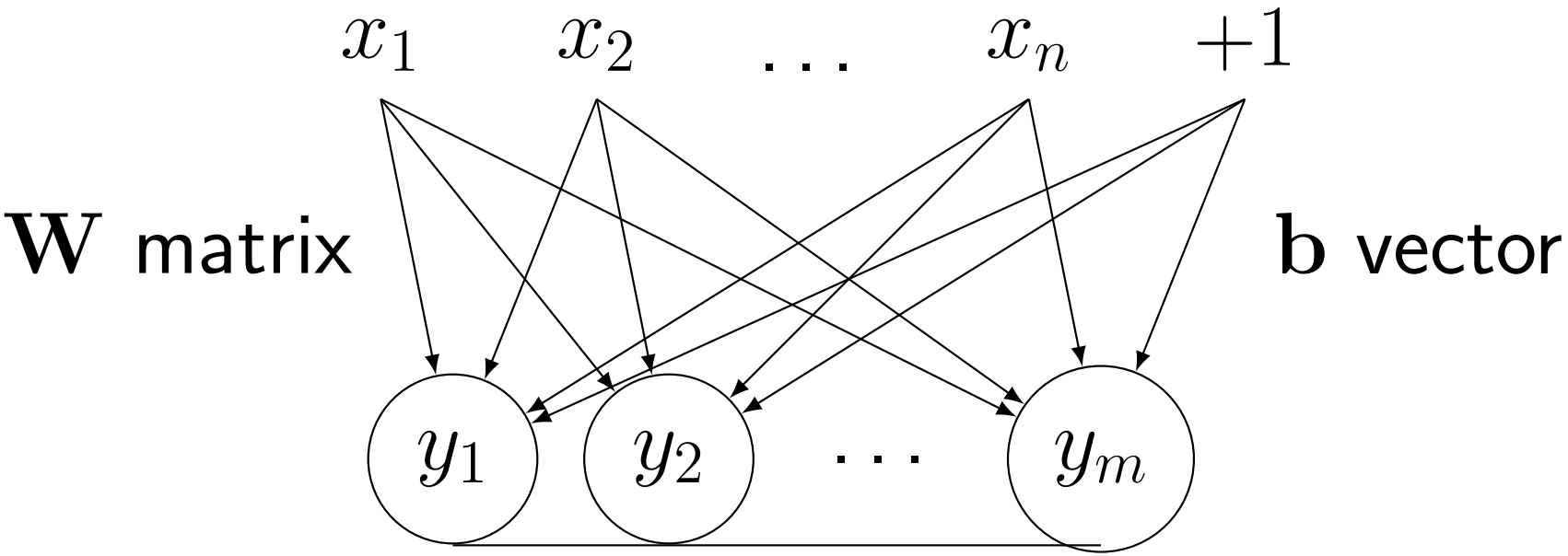
# Binary Classification with One Layer

- same as binary logistic regression



# Multinomial Logistic Regression

- achieved with one-layer classification




simple sum + softmax

$$\mathbf{y} = \text{softmax}(\mathbf{W}\mathbf{x} + \mathbf{b})$$

# Softmax Function

- Softmax transforms numbers into positive domain using $e^x$; i.e., $\exp(x)$, function, and normalizing numbers into a probability distribution

$$\text{softmax}(\mathbf{x}) = [\frac{\exp(x_1)}{\sum_{i=1}^{n}\exp(x_i)}, \frac{\exp(x_2)}{\sum_{i=1}^{n}\exp(x_i)}, \cdots \frac{\exp(x_n)}{\sum_{i=1}^{n}\exp(x_i)}]$$

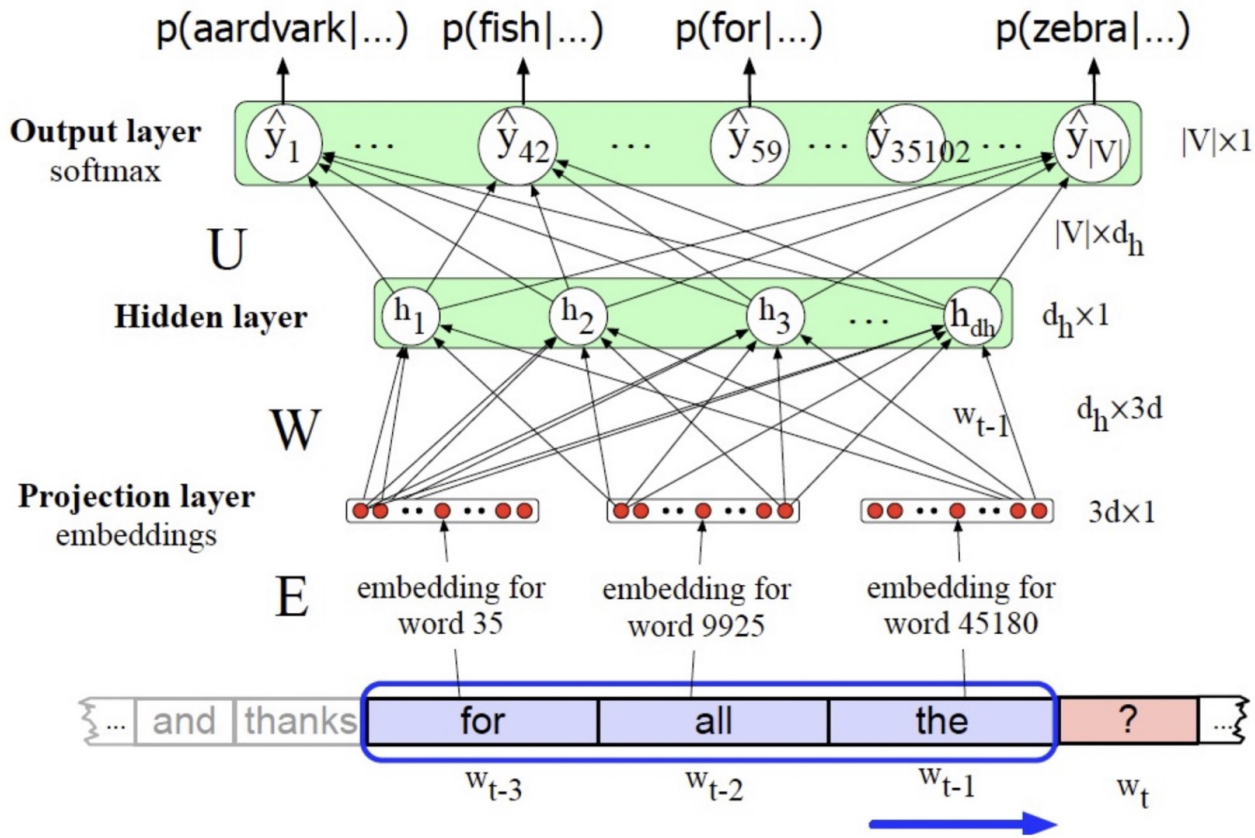
$$\text{softmax}(x_i) = \frac{\exp(x_i)}{\sum_{j=1}^{n}\exp(x_j)}$$

- Example from Jurafsky and Martin:

$$\mathbf{x} = [0.6, 1.1, -1.5, 1.2, 3.2, -1.1]$$

$$\text{softmax}(x) = [0.055, 0.09, 0.006, 0.099, 0.74, 0.01]$$

# Neural Language Model

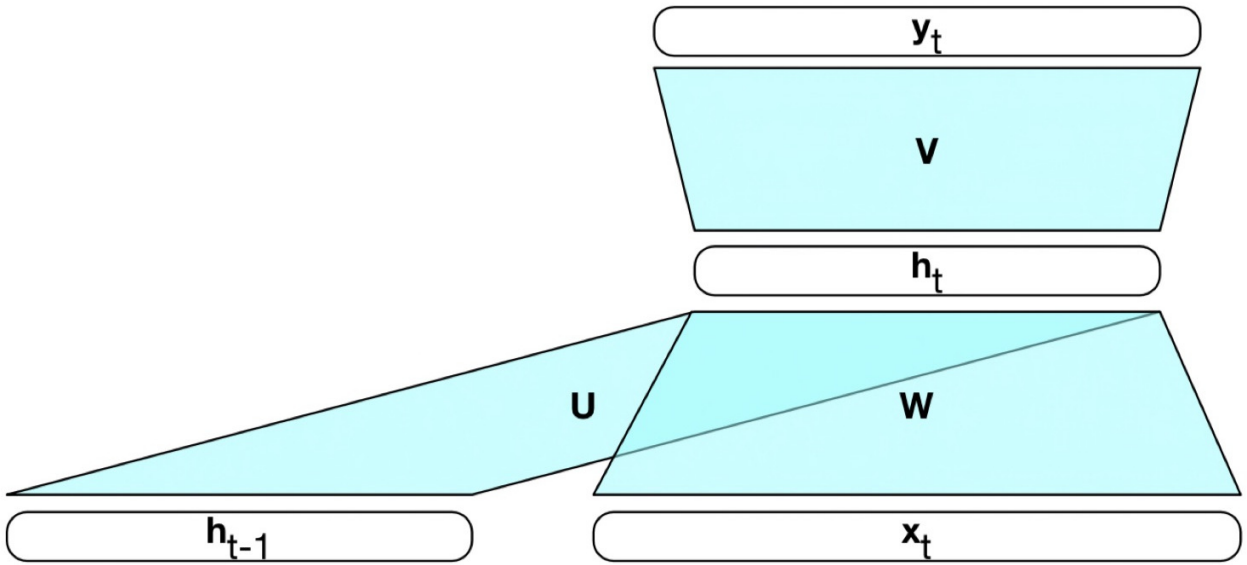



(Jurafsky and Martin)

The model has limited history, similarly to n-gram model

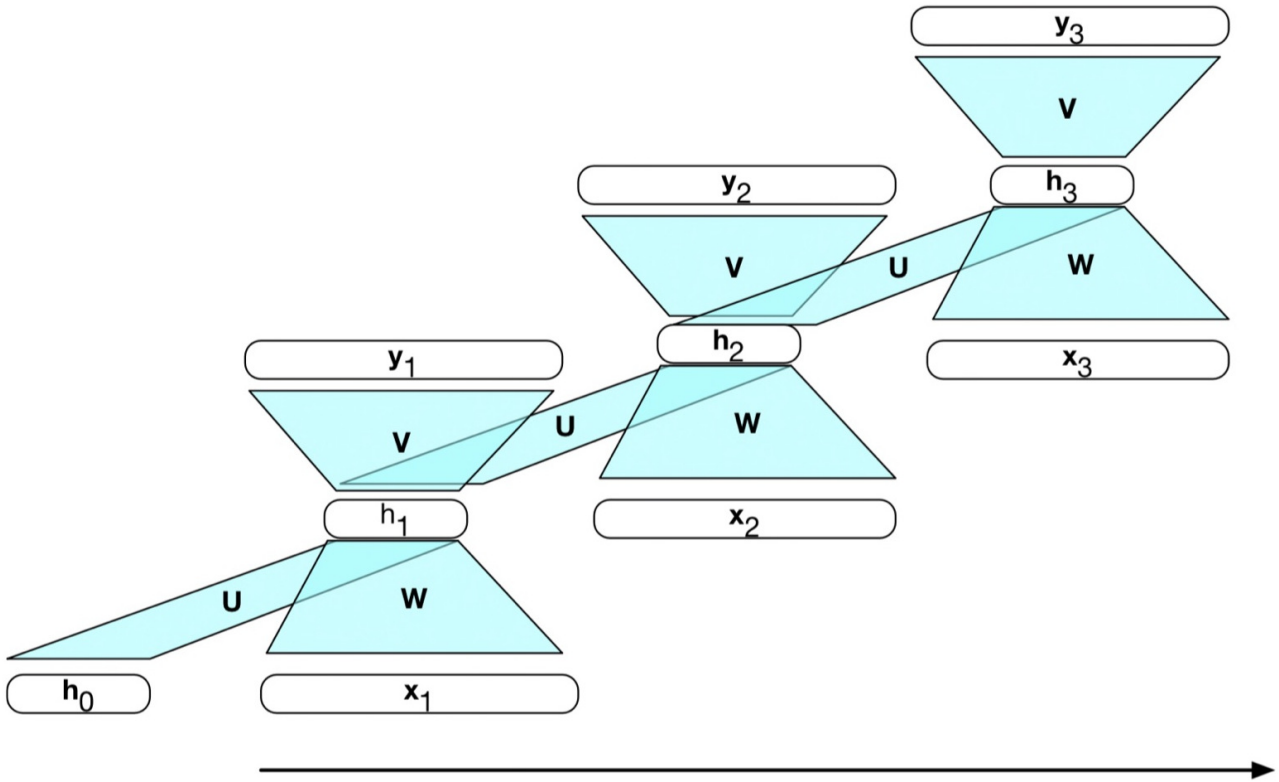
# Recurrent Neural Networks (RNN)

- Simple recurrent neural network presented as a feedforward network (Jurafsky and Martin)
- RNN is trained as a Language model by providing the next word as output



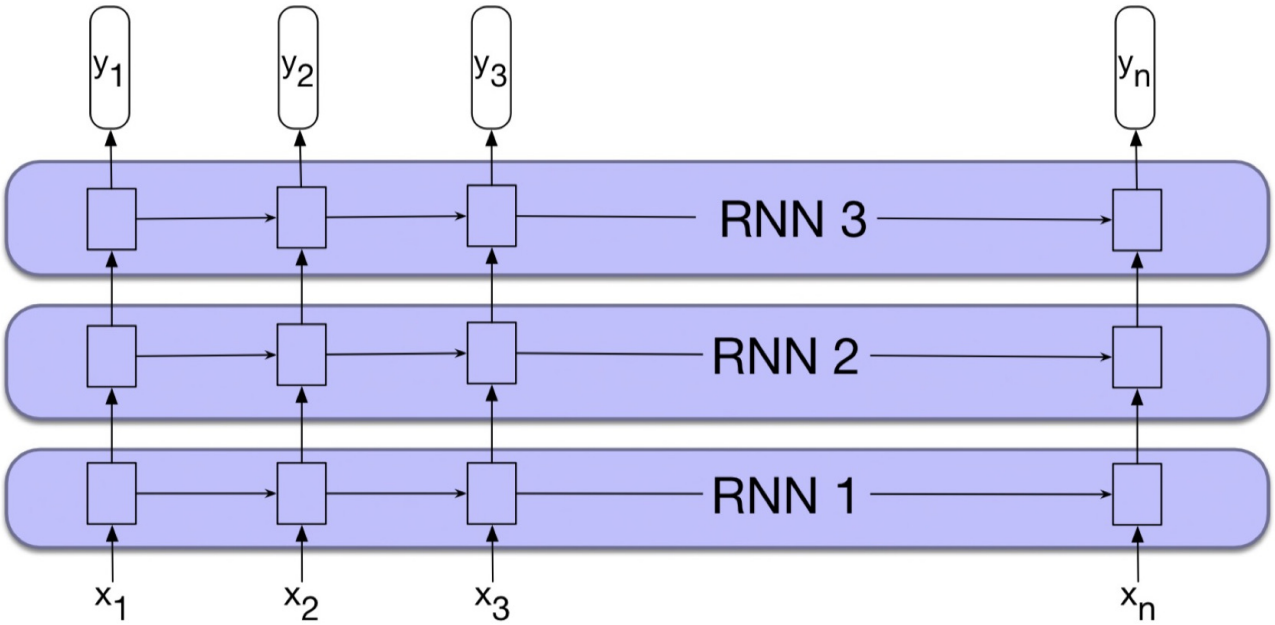
# RNN Unrolled in Time

- RNN unrolled in time; more clear view of training (Jurafsky and Martin)



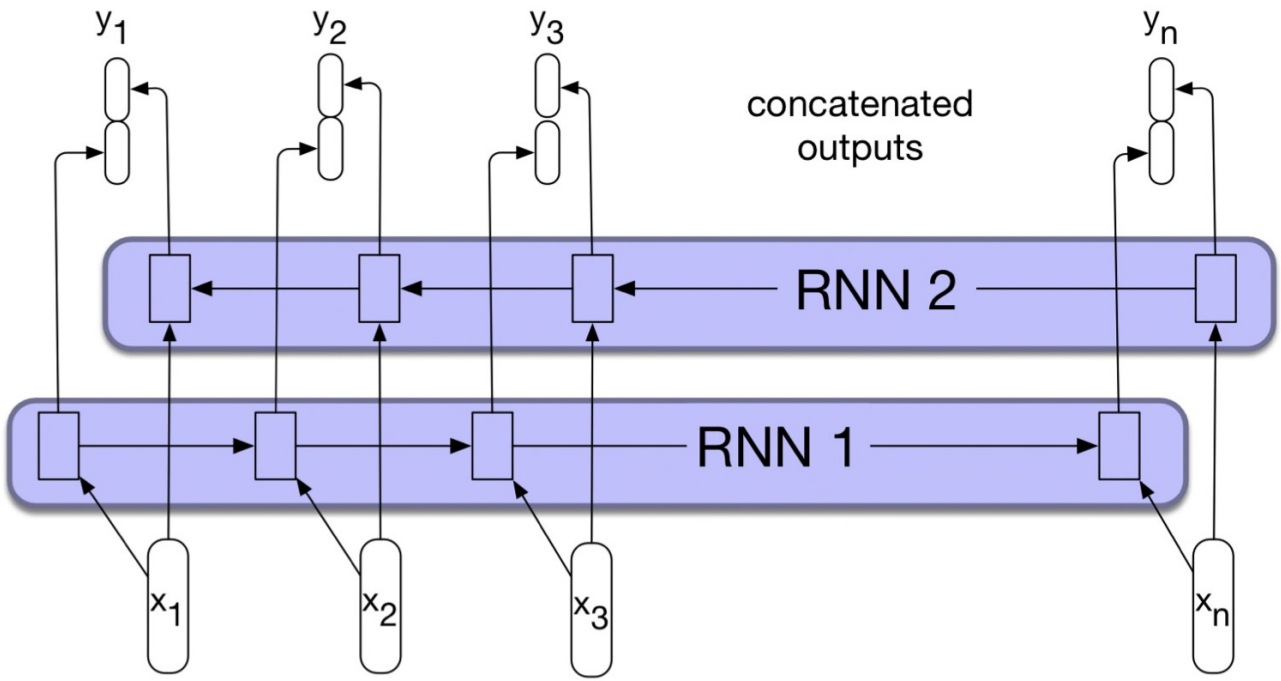
# Stacked RNN

- Stacked RNN: Output from lower level is input to higher level; top level is final output (Jurafsky and Martin)



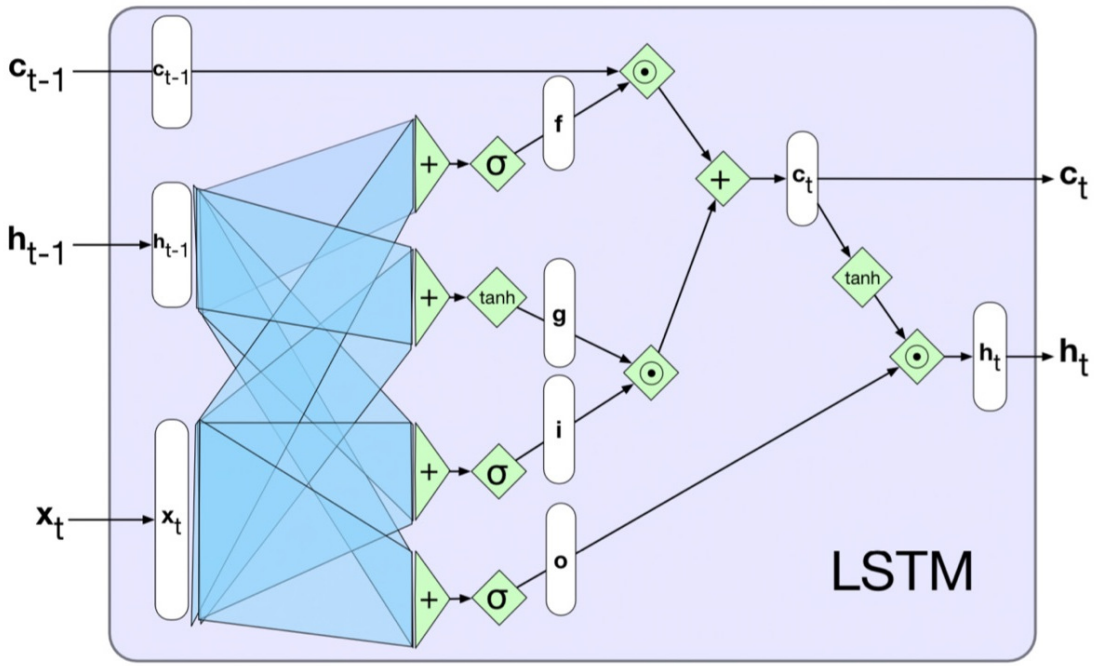
# Bidirectional RNN

- Bidirectional RNN; trained forward and backward with concatenated output (Jurafsky and Martin)
- Output can be used for sequence labeling, for example



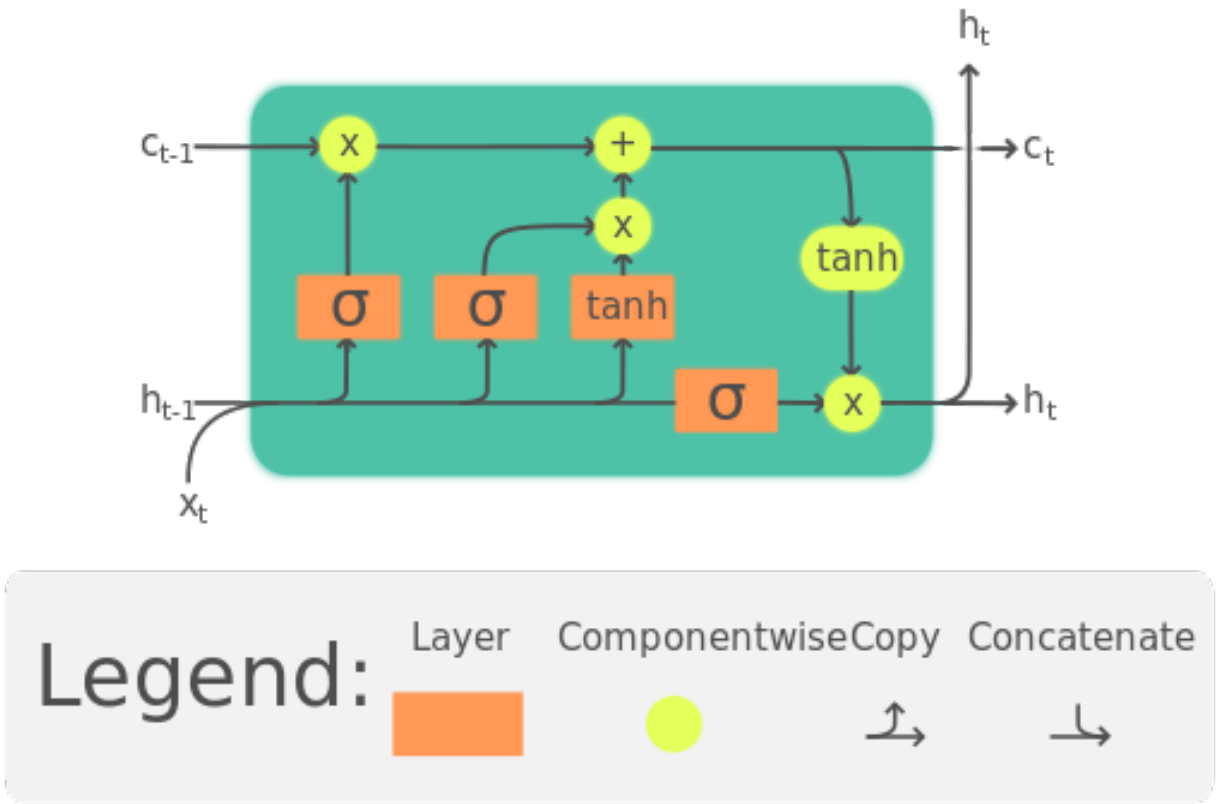
# LSTM — Long Short-Term Memory

- LSTM: $x_t$ is input, $h_{t-1}$ is previous hidden state, $c_{t-1}$ is previous long-term context, $h_t$ and $c_t$ is output (Jurafsky and Martin)



# LSTM Cell

- Another view of LSTM cell (source Wikipedia)



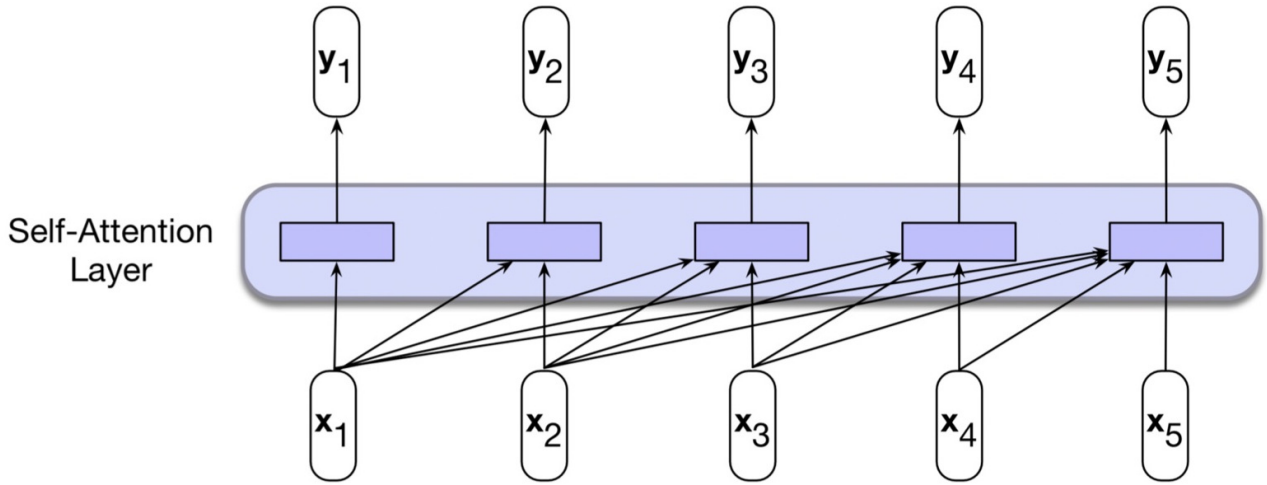
# Transformers

- Transformers map a sequence of input vectors to a sequence of output vectors of the same length

$$\begin{array}{cccc} x_1 & x_2 & \dots & x_n \\ \hline \downarrow & \downarrow & \vdots & \downarrow \\ \hline y_1 & y_2 & \dots & y_n \end{array}$$

- Appeared around 2017

# Self-Attention Layer




(Jurafsky and Martin)

# Self-Attention Training

- A simplified view:

$$\textit{score}(x_i, x_j) = x_i \cdot x_j$$

$$\alpha_{ij} = \text{softmax}(\textit{score}(x_i, x_j)) \quad \forall j \leq i$$

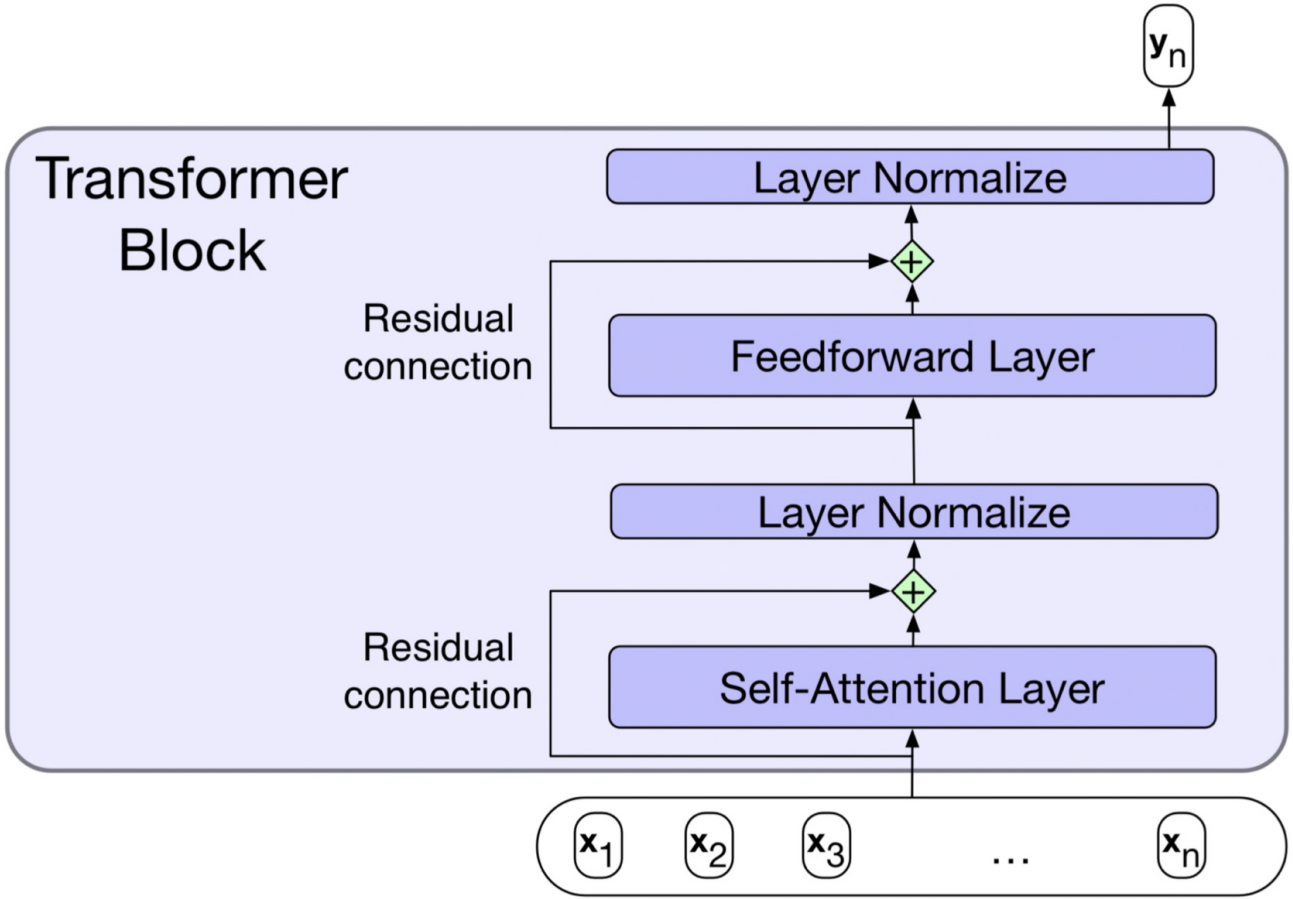
$$y_i = \sum_{j \leq i} \alpha_{ij} x_j$$

# Actual Attention Computation

- Three separate roles for each word vector:

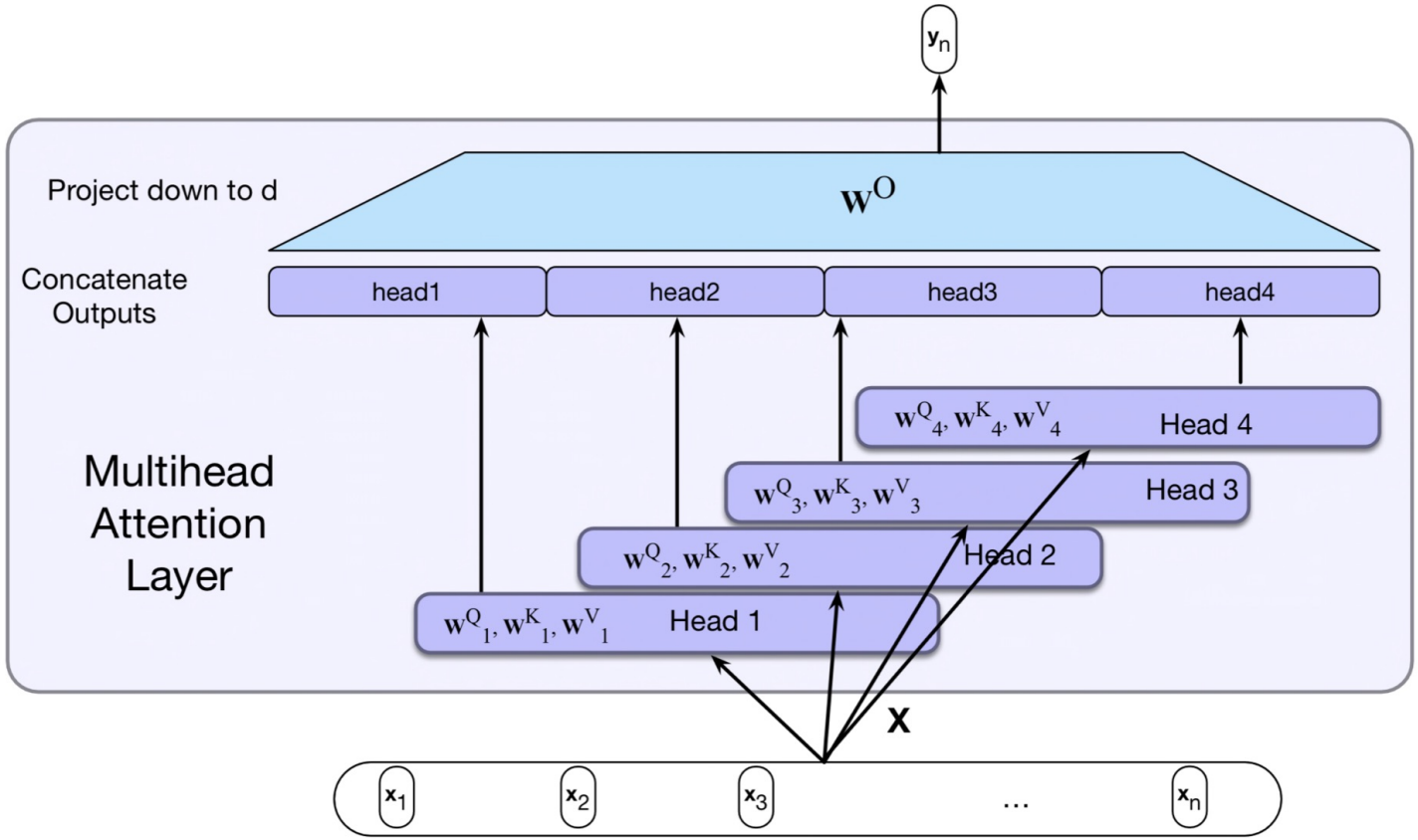
1. query: current token being compared to preceding tokens
2. key: preceeding token being compared to the current
3. value: value of a preceding token that gets weighted

# Transformer Block




(Jurafsky and Martin)

# Multihead Attention Layer




(Jurafsky and Martin)

# Encoding Word Positions in Transformers

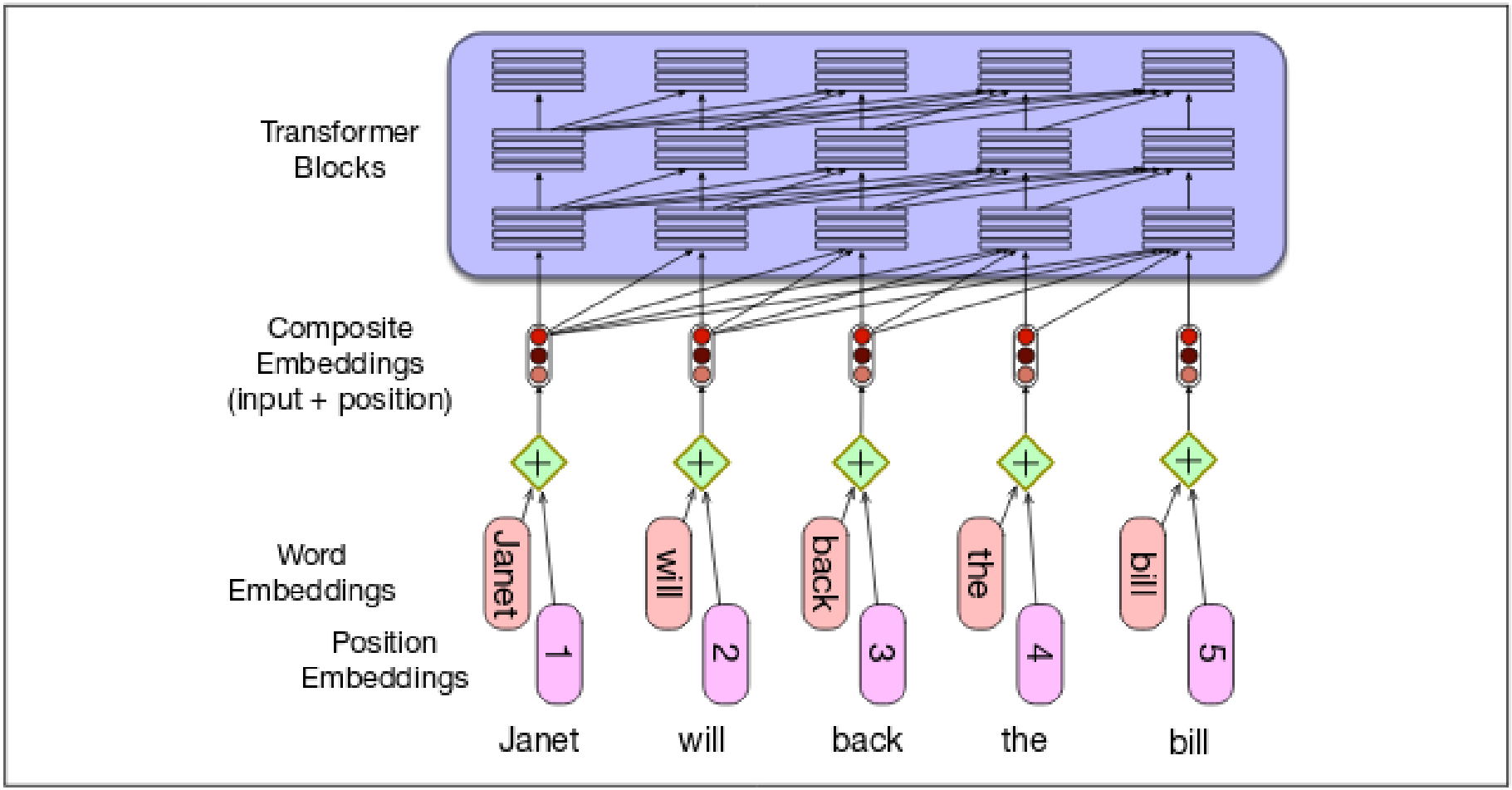



**Figure 9.20** A simple way to model position: simply adding an embedding representation of the absolute position to the input word embedding.

from: Jurafsky and Martin, 3rd ed. draft

# Training Transformer as a Language Model

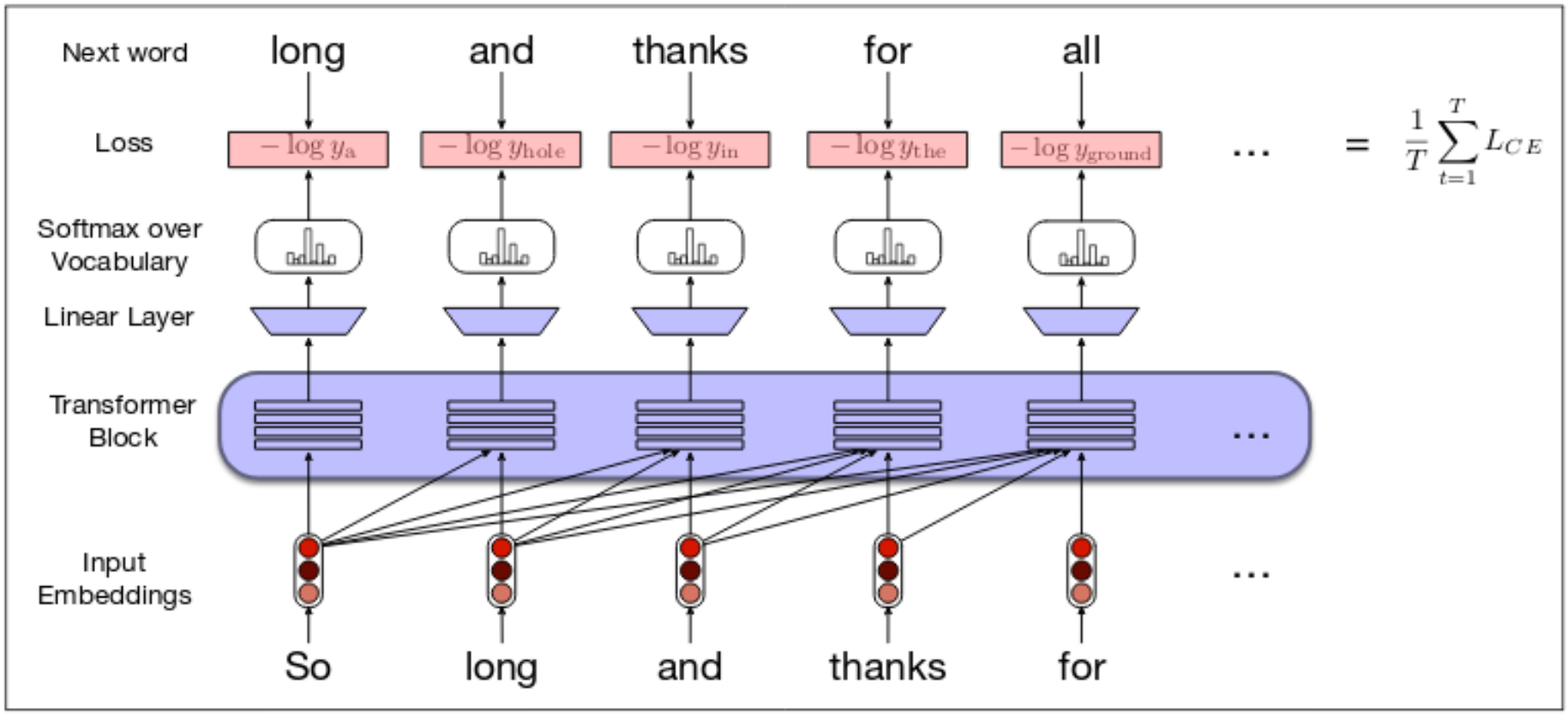



**Figure 9.21** Training a transformer as a language model.

from: Jurafsky and Martin, 3rd ed. draft

# Text Completion with Transformers

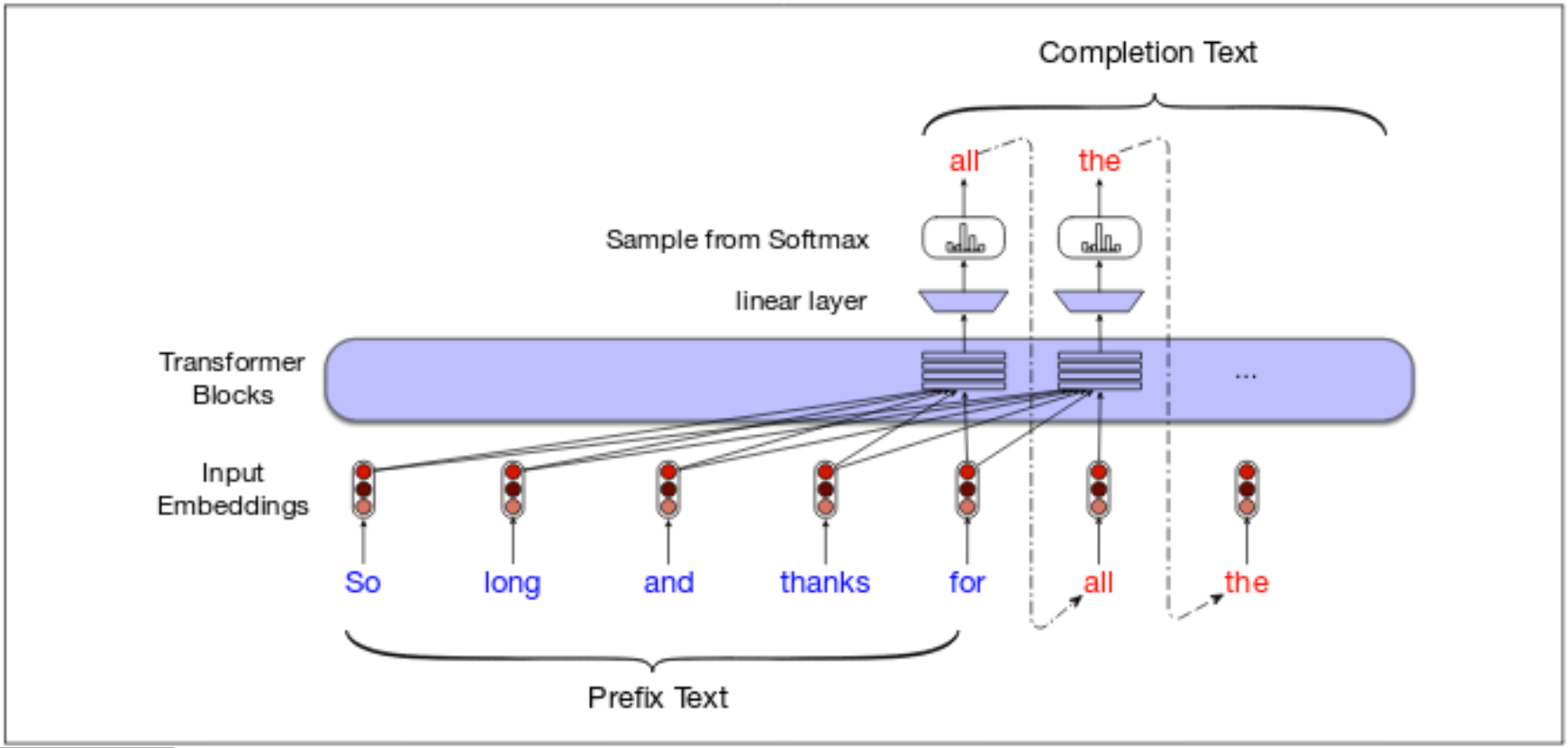



**Figure 9.22** Autoregressive text completion with transformers.

from: Jurafsky and Martin, 3rd ed. draft

# Parsing Natural Languages

# Parsing Natural Languages

- Must deal with possible ambiguities
- Decide whether to make a phrase structure or dependency parser
- When parsing NLP, there are generally two approaches:
  1. Backtracking to find all parse trees
  2. Chart parsing
- Prolog provides a very expressive way to NL parsing
- FOPL is also used to represent semantics

# Parsing with Prolog

- We will go over a brief Prolog review
  - more details are provided in the lab
- Implicative normal form:

$$p_1 \wedge p_2 \wedge \ldots \wedge p_n \Rightarrow q_1 \vee q_2 \vee \ldots \vee q_m$$

- If $m \leq 1$, then the clause is called a **Horn clause.**
- If resolution is applied to two Horn clauses, the result is again a Horn clause.
- Inference with Horn clauses is relatively efficient

# Rules

A Horn clause with $m = 1$ is called a **rule**:

$$p_1 \wedge p_2 \wedge \ldots \wedge p_n \Rightarrow q_1$$

It is expressed in Prolog as: `q1 :- p1, p2, ..., p_n.`

# Facts

A clause with $m = 0$ is called a **fact**:

$$p_1 \wedge p_2 \wedge \ldots \wedge p_n \Rightarrow \top$$

is expressed in Prolog as: `p1, p2, ..., p_n.`
or `:- p1, p2, ..., p_n.`
and it is called a **fact.**

# Rabbit and Franklin Example

The 'rabbit and franklin' example in Prolog:

```
hare(rabbit).
turtle(franklin).
faster(X,Y) :- hare(X), turtle(Y).
```

Save the program in a file, load the file.

After loading the file, on Prolog prompt, type:

```
faster(rabbit,franklin).
```

Try: `faster(X,franklin).` and `faster(X,Y).`

# Rabbit and Franklin Example

```
hare(rabbit).
turtle(franklin).
faster(X,Y) :- hare(X), turtle(Y).

?- faster(rabbit,franklin).
```

# Rabbit and Franklin Example

```
hare(rabbit).
turtle(franklin).
faster(X,Y) :- hare(X), turtle(Y).

?- faster(X,franklin).
```

# Rabbit and Franklin Example

```
hare(rabbit).
turtle(franklin).
faster(X,Y) :- hare(X), turtle(Y).

?- faster(X,Y).
```

# Unification and Backtracking

- Two important features of Prolog: unification and backtracking
- Prolog expressions are generally mathematical symbolic expressions, called *terms*
- **Unification** is an operation of making two terms equal by substituting variables with some terms
- **Backtracking:** Prolog uses backtracking to satisfy given goal; i.e., to prove given term expression, by systematically trying different rules and facts, which are given in the program

# Example in Unification and Backtracking

- What happens after we type:
  `?- faster(rabbit,franklin).`
- Prolog will search for a 'matching' fact or head of a rule:
  `faster(rabbit,franklin)` and
  `faster(X,Y) :- ...`
- 'Matching' here means **unification**
- After unifying `faster(rabbit,franklin)` and `faster(X,Y)` with substitution `X`←`rabbit` and `Y`←`franklin`, the rule becomes:

```
faster(rabbit,franklin) :-
    hare(rabbit), turtle(franklin).
```

# Example (continued)

- Prolog interpreter will now try to satisfy predicates at the right hand side: `hare(rabbit)` and `turtle(franklin)` and it will easily succeed based on the same facts
- If it does not succeed, it can generally try other options through **backtracking**

# Variables in Prolog

- Variable names start with uppercase letter or underscore ('_')
- _ is a special, *anonymous variable*
- Examples: `?- faster(rabbit,franklin).`

```
Yes ;
...
?- faster(rabbit,X).
X = franklin ;
...
?- hare(X).
X = rabbit ;
```

# Lists (Arrays), Structures.

Lists are implemented as linked lists. Structures (records) are expressed as terms. Examples:
In program: `person(john,public,'123-456').`
Interactively: `?- person(john,X,Y).`
`[]` is an empty list.
A list is created as a nested term, usually a special function '.' (dot):

```
?- is_list(.(a, .(b, .(c, [])))).
```

# List Notation

`(.(a, .(b, .(c, [])))` is the same as `[a,b,c]`

This is also equivalent to:

```
[ a | [ b | [ c | [] ]]]
```

or

```
[ a, b | [ c ] ]
```

A frequent Prolog expression is: `[H|T]`

where H is head of the list, and T is the tail, which is another list.

# Example: Calculating Factorial

```
factorial(0,1).
factorial(N,F) :- N>0, M is N-1, factorial(M,FM),
    F is FM*N.
```

After saving in `factorial.prolog` and loading to Prolog:

```
?- ['factorial.prolog'].
% factorial.prolog compiled 0.00 sec, 1,000 bytes

Yes
?- factorial(6,X).

X = 720 ;
```

# Example: List Membership

Example (testing membership of a list):

```
member(X, [X|_]).
member(X, [_|L]) :- member(X,L).
```